

# Product yields for the photofission of $^{232}\text{Th}$ , $^{234,238}\text{U}$ , $^{237}\text{Np}$ , and $^{239,240,242}\text{Pu}$ actinides at various incident photon energies

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**Abstract** Photofission fragments mass yield for  $^{232}\text{Th}$ ,  $^{234,238}\text{U}$ ,  $^{237}\text{Np}$ , and  $^{239,240,242}\text{Pu}$  isotopes are investigated. The calculations are done using a developed approach based on Gorodisskiy's phenomenological formalism. The Gorodisskiy's method is developed to be applied for the neutron-induced fission. Here we revised it for application to photofission. The effect of emitted neutron prior to fission on the fission fragment mass yields has also been studied. The peak-to-valley ratio is extracted for the  $^{240}\text{Pu}$  isotope as a function of energy. Obtained results of the present formalism are compared with the available experimental data. Satisfactory agreement is achieved between the results of present approach and the experimental data.

**Keywords** Fission fragments · Fragment mass yield · Photofission · Neutron fission · Heavy nuclei · Peak-to-valley

## 1 Introduction

In spite of peaceful application in energy production, different features of various kinds of fission are not known yet. Photofission is one way to induce fission on actinides (U, Pu, Np, etc.). Although photofission was discovered more than fifty years ago [1], its theoretical modeling was produced with many challenges. Various theoretical approaches [2–7] have been presented to evaluate fragment

mass yields for neutron(proton)-induced fission, but there is no comprehensive method to study photofission. The distribution of fragment mass yield plays a significant role in examining the validity of every theoretical method of fission. If the calculated fragment mass yields are well fitted with measured data, this means that the selected model is suitable to be applied for the fission process. In the statistical model of Wilkins [8, 9] and its developed version by Moreau [10], the probability of fission for neutron-induced fission is presented as follows:

$$P \sim e^{(-E_{\text{total}}/T)} = e^{(-(E_{\text{mac}}+E_{\text{mic}})/T)}, \quad (1)$$

where  $P$  is the probability of fission and  $E_{\text{total}}$  includes all kinds of energies presented in the evaluation of compound nucleus from saddle to scission point.  $E_{\text{mac}}$  and  $E_{\text{mic}}$  are the macroscopic and microscopic energies, respectively. The relation between fission fragments mass yield and fragment mass number indicates that the probability appears in the Gaussian form. Therefore, the theoretical neutron-induced fission models are developed in the form of a multi-Gaussian shape and are formulated as a sum of several Gaussian-type function [11–13].

The old formalism presented by Wang Fu-cheng [5] was applicable for reproducing low-energy fission and contains five Gaussian terms. The formalism of Robert Mills [14], in which the dependence on energy was neglected, includes four Gaussian terms in the quadratic structure. The GEF computer code [15] is developed based on this method with various assumptions and many adjustable parameters. The complicated Langevin–Brownian method has been employed to study neutron-induced fission and lunched some success in recent years [16–21]. Recently, the Gorodisskiy phenomenological method [22] has been successful in reproducing the experimental data for

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neutron-induced fission of actinides. It is clear that the photofission process is similar to neutron-induced fission except in multi-polarity absorptions and time scale of the fission process. These absorptions happen in the beginning of the process; therefore, after formation of the compound nucleus, the fission process of the neutron-induced fission will become similar to photofission. According to the Bohr's hypothesis, the compound nucleus rapidly loses its total formation memory except conserved degrees of freedom. Therefore, the mode of decay of the compound nucleus does not depend on the way the compound nucleus is formed. Thus, for the same excited configuration of the compound nucleus, the photofission fragment mass yield is expected to be approximately similar to the neutron-induced fission. In the present study, we examined an extended version of the Gorodisskiy's method to generate the photofission fragment mass yield. The relative contributions of the symmetric and the asymmetric yields ( $Y_s$  and  $Y_a$ ) of the Gorodisskiy's method and the variance of asymmetric fission ( $\sigma_a$ ) are modified. The detail of modification is presented in the next section. The paper is constructed as follows: Theoretical model used to calculate the fission fragments mass distribution is presented in Sect. 2. In Sect. 3, theoretical results are compared with the experimental data for different excitation energies and different numbers of emitted neutron prior to fission for  $^{232}\text{Th}$ ,  $^{234,238}\text{U}$ ,  $^{237}\text{Np}$ , and  $^{239,240,242}\text{Pu}$  actinides. Finally, a short conclusion is presented in Sect. 4.

## 2 Description of theoretical model

Studies of fission fragments mass distribution of most fissioning nuclei indicate that the yield of fission fragments as a function of fragment mass number ( $A$ ) is a Gaussian function with 4 [24] or 3 [23] modes. These modes are symmetric ( $SL$ ) or asymmetric ( $S1$ ,  $S2$ , and  $S3$ ) related to the type of the compound nucleus and its excitation energy.

In the Gorodisskiy's original approach that has developed for neutron-induced fission, two main parts are considered to generate the mass distribution of fission fragments. The yield of fragment with mass number higher than the half of compound nucleus is indicated by  $Y_H$ , and its conjugate with the mass number lower than the half of compound nucleus is indicated with  $Y_L$ . These modes are presented as an exponential function with a small deviation from Gaussian shape. Therefore, it is convenient to use the Charlier's distribution [22, 25, 26] to construct the fission fragment mass yield

$$f(u) = 1 - \gamma_1 \left( \frac{1}{2}u - \frac{1}{6}u^3 \right) + \gamma_2 \left( \frac{1}{24}u^4 - \frac{1}{4}u^2 + \frac{1}{8} \right), \quad (2)$$

where  $u = \frac{(M - \langle M \rangle)}{\sigma}$  and coefficients  $\gamma_1$  and  $\gamma_2$  are, respectively, called dissymmetry and excess and are given by

$$\begin{aligned} \gamma_1 &= \frac{\langle (M - \langle M \rangle)^3 \rangle}{\sigma^3} \\ \gamma_2 &= \frac{\langle (M - \langle M \rangle)^4 \rangle}{\sigma^4} - 3. \end{aligned} \quad (3)$$

When  $\gamma_1 = \gamma_2 = 0$ , the value of Charlier's distribution is equal to one. Values of these parameters for different actinides with their given atomic number are presented in Table 1 [22].

In the original approach of Gorodisskiy, the yield of heavy fragment is defined by the following relation

$$Y_H = \frac{1}{\sqrt{2\pi}} \left( \frac{Y_s e^{-1/2 u_s^2}}{\sigma_s} + \frac{Y_a e^{-1/2 u_a^2} f(u)}{\sigma_a} \right), \quad (4)$$

where  $Y_s$  and  $Y_a$ , respectively, correspond to the relative contributions of the symmetric and asymmetric modes of fission in the fragments yield, respectively. Parameters  $\gamma_1$  and  $\gamma_2$  are adjusted with the experimental data for each compound nucleus formed after absorption of photon [22]. Also,  $u_a$ ,  $u_s$ ,  $\sigma_a$ , and  $\sigma_s$  are defined as follows:

$$\sigma_a = \frac{(A_{cn} - v_{pre})(Z_{cn} - 73)(0.074 + 0.0296\sqrt{E})}{Z_{cn}}, \quad (5)$$

$$\sigma_s = \frac{0.031 (A_{cn} - v_{pre}) \sqrt[4]{E}}{\sqrt{90.54 - 1.9 \frac{Z_{cn}^2}{A_{cn} - v_{pre}}}} + 9.64, \quad (6)$$

$$u_s = \frac{A - (A_{cn} - v_{pre})/2}{\sigma_s} \quad (7)$$

and

$$u_a = \frac{A - \alpha}{\sigma_a}. \quad (8)$$

where  $\alpha = 54 \frac{A_{cn} - v_{pre}}{Z_{cn}}$  for  $Z_{cn} = 90-91$  and  $\alpha = 28.6 \frac{A_{cn} - v_{pre}}{Z_{cn}} + 0.708 Z_{cn}$  for  $Z_{cn} \geq 92$ .  $A_{cn}$  and  $Z_{cn}$  are, respectively, the mass and charge numbers of compound nucleus.  $v_{pre}$  is the average pre-scission neutron multiplicity and  $E$  is the gamma-rays energy. Also,  $A$  is the mass number of the nascent fragment. In order to calculate the values of  $Y_a$  and

**Table 1** Values of  $\gamma_1$  and  $\gamma_2$  for various actinides with definite  $Z_{cn}$

$Z_{cn}$	90	91	92	93	94	95
$\gamma_1$	0	- 0.08	0.36	0.23	0.3	0.38
$\gamma_2$	- 0.36	- 0.07	- 0.34	- 0.27	- 0.3	- 0.34

$Y_s$  in Eq. (3), the ratio  $\frac{Y_a}{Y_s}$  is obtained through the fitting method with the experimental data as follows:

$$\frac{Y_a}{Y_s} = 1.244 \left( 1 - e^{-0.0027(|E-5.7|)^{3/2}} \right) \left( \sqrt{E} + 100 \left( \frac{Z_{cn}}{A_{cn}} - 0.4 \right) \right), \quad (9)$$

and the values of  $Y_a$  and  $Y_s$  are obtained by replacing this ratio in the following equations

$$Y_a = 200 \left( \left| \frac{Y_a}{Y_s} \right| + 2 \right)^{-1} \quad (10)$$

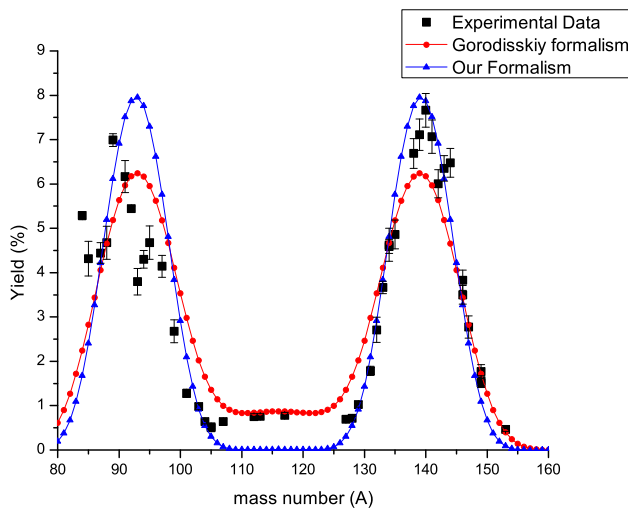
and

$$Y_s = 200 - 2Y_a. \quad (11)$$

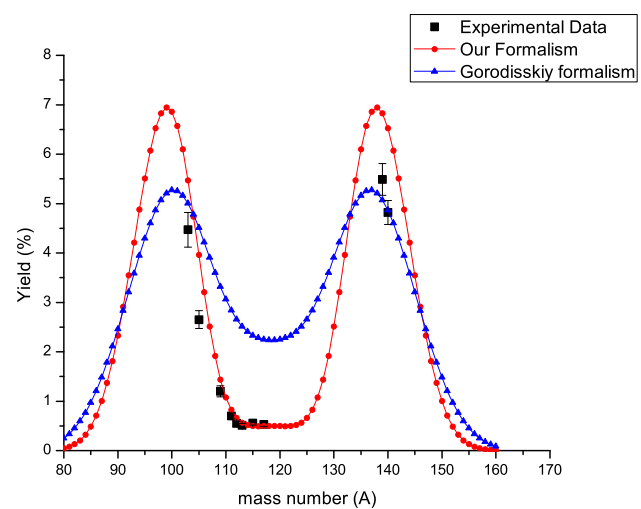
In a similar way, the yield of light conjugate fragment ( $Y_L$ ) is also obtained by replacing  $M_L$  with  $A_{cn} - A$ . Finally, the fission fragment mass yield is evaluated using the following equation

$$Y = Y_H + Y_L. \quad (12)$$

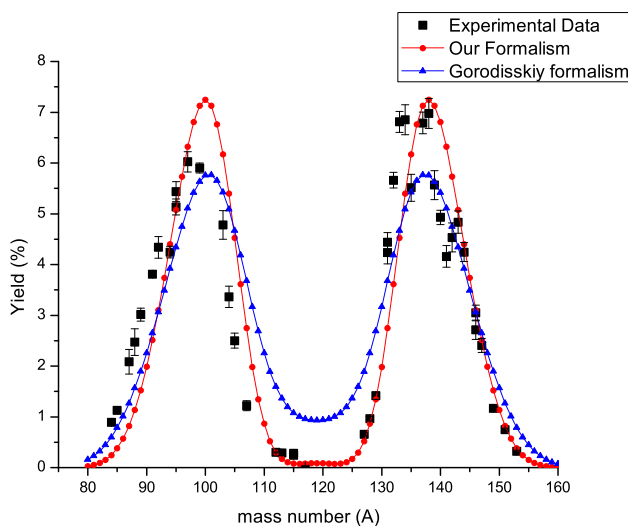
Equation (9) is revised by considering two adjustable parameters  $\beta$  and  $\delta$ , instead of their fixed values in the original formalism of Gorodisskiy as,



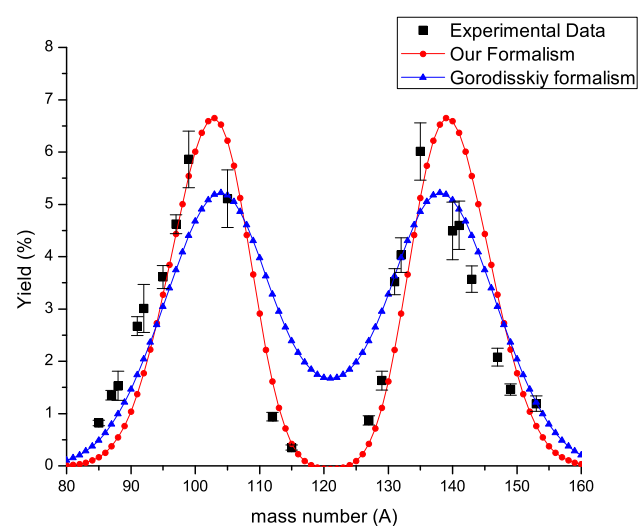
**Fig. 1** (Color online) Photofission fragment mass yield at 16 MeV for  $^{232}\text{Th}$ : comparison between the experimental data [28], the results of Gorodisskiy's formalism and the results of present study



**Fig. 3** (Color online) Photofission fragment mass yield at 24 MeV for  $^{237}\text{Np}$ : comparison between the experimental data [34], the results of Gorodisskiy's formalism and the results of present study



**Fig. 2** (Color online) Photofission fragment mass yield at 17.2 MeV for  $^{238}\text{U}$ : comparison between the experimental data [31], the results of Gorodisskiy's formalism and the results of present study



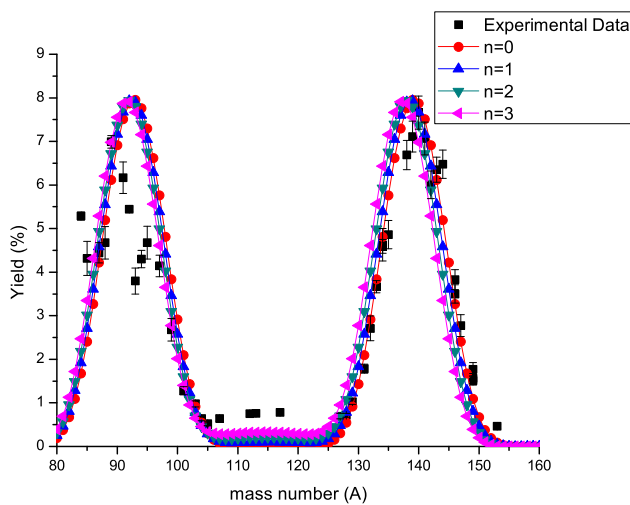
**Fig. 4** (Color online) Photofission fragment mass yield at 20 MeV for  $^{242}\text{Pu}$ : comparison between the experimental data [38], the results of Gorodisskiy's formalism and the results of present study

$$\frac{Y_a}{Y_s} = 1.244 \left( 1 - e^{-0.0027(|E-5.7|)^\delta} \right) \left( \sqrt{E} + 100 \left( \frac{Z_{cn}}{A_{cn}} - 0.4 \right) \right). \quad (13)$$

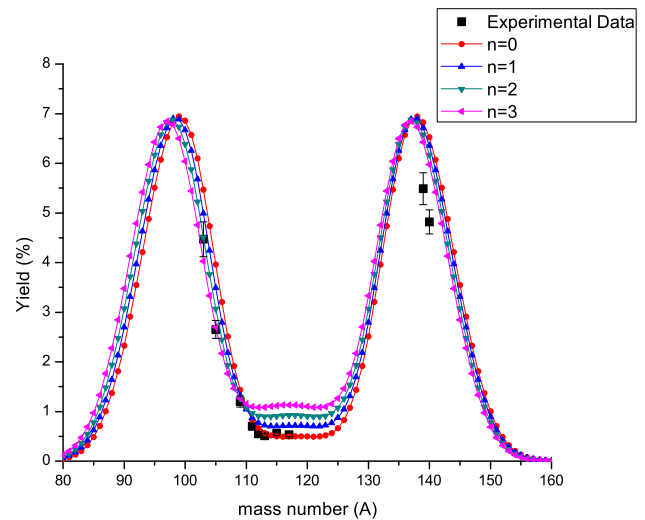
The parameters  $\beta$  and  $\delta$  are obtained using the fitting method with experimental data. The developed approach is used to calculate the photofission fragment mass yield of various actinides at different energies.

### 3 Results and discussion

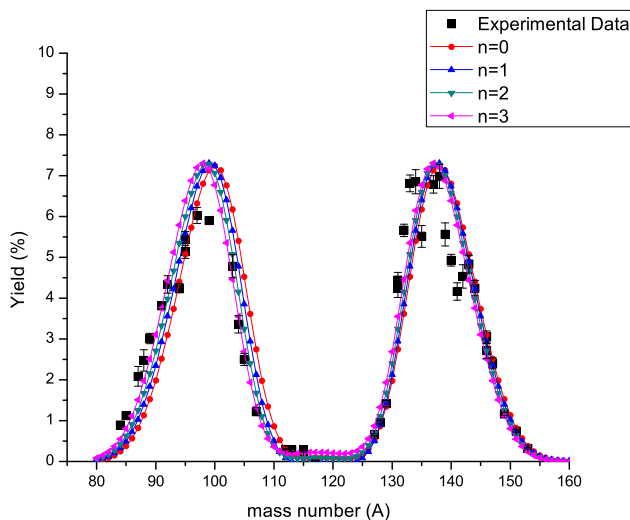
The revised formalism presented in this paper is applied to calculate the fragments mass distribution in photofission reactions of  $^{232}\text{Th}$  at 16 MeV,  $^{238}\text{U}$  at 17.2 MeV,  $^{237}\text{Np}$  at 24 MeV, and  $^{242}\text{Pu}$  at 20 MeV and compared with the results of Gorodisskiy's formalism as well as the experimental data in Figs. 1, 2, 3 and 4. As it is clear from Figs. 1, 2, 3 and 4, the fission fragment mass yields of the present formalism are in better agreement with experimental data than the Gorodisskiy's original formalism. However, there is some



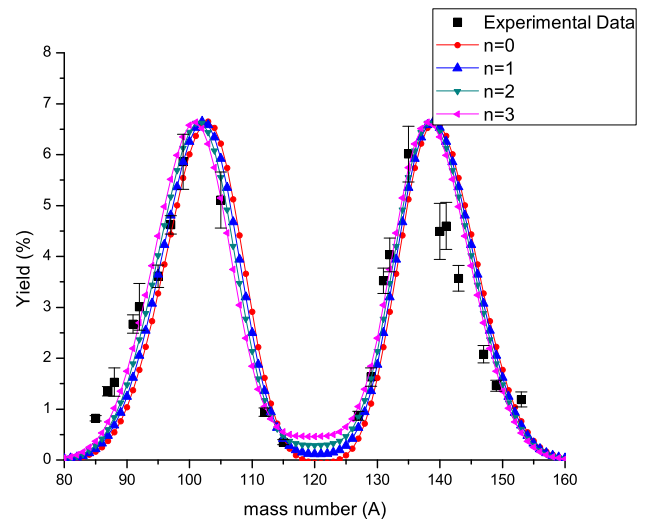
**Fig. 5** (Color online) Photofission fragments mass yield at 14 MeV for  $^{232}\text{Th}$ : comparison between the experimental data [28] and the results of present study by considering 1, 2, and 3 neutrons emitted prior to fission



**Fig. 7** (Color online) Photofission fragment mass yield at 24 MeV for  $^{237}\text{Np}$ : comparison between the experimental data [34] and the results of present study by considering 1, 2, and 3 neutrons emitted prior to fission



**Fig. 6** (Color online) Photofission fragment mass yield at 17.2 MeV for  $^{238}\text{U}$ : comparison between the experimental data [31] and the results of present study by considering 1, 2, and 3 neutrons emitted prior to fission



**Fig. 8** (Color online) Photofission fragment mass yield at 20 MeV for  $^{242}\text{Pu}$ : comparison between the experimental data [38] and the results of present study by considering 1, 2 and 3 neutrons emitted prior to fission

inconsistency between the calculated results and the experimental data especially in the most probable fragmentation, around the maximum of fragment yields.

In Figs. 5, 6, 7 and 8, the calculated results of fission fragment yields considering 1, 2, 3 and 4 pre-scission neutron multiplicity prior to fission are compared with the experimental data for photofission reactions of  $^{232}\text{Th}$  at 14 MeV,  $^{238}\text{U}$  at 17.2 MeV,  $^{237}\text{Np}$  at 24 MeV, and  $^{242}\text{Pu}$  at 20 MeV. These figures indicate that the emission of neutrons prior to fission does not considerably affect the photofission fragment mass yield. This is one of the Gorodisskiy formalisms drawbacks that is not able to properly indicate the role played by neutron emission in photofission. In order to calculate the fission fragment mass yield as a function of fragment atomic number, ( $Z$ ), following the semiempirical formula between the fragment mass, ( $A$ ) and its atomic number, ( $Z$ ) is employed

$$A = \frac{A_{\text{cn}}}{Z_{\text{cn}}} (Z - 2.5). \quad (14)$$

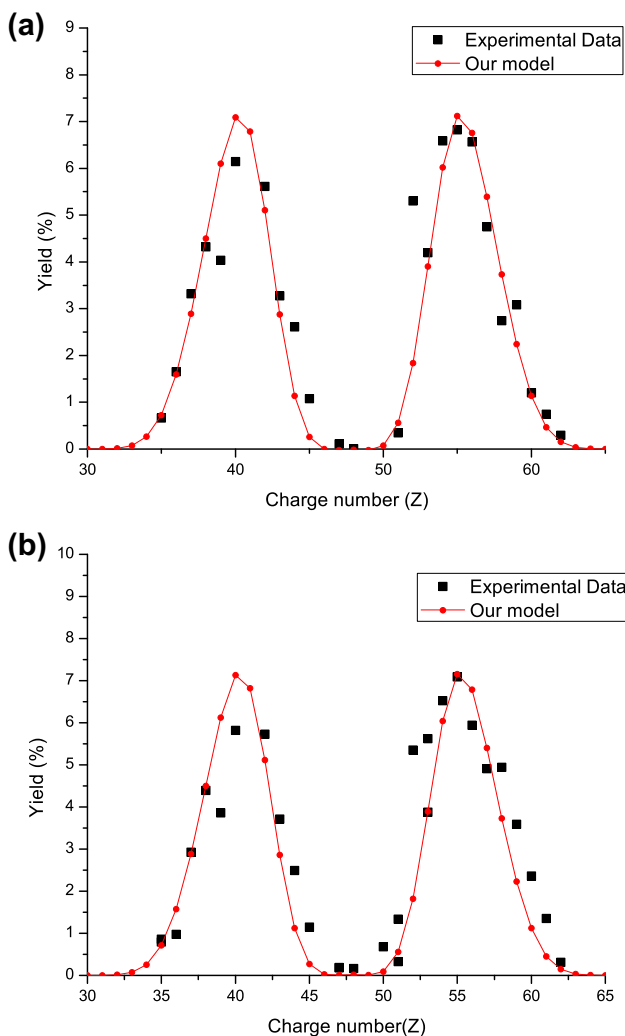
The fragment mass yield of photofission for  $^{238}\text{U}$  at 11.39 MeV and 13.39 MeV is calculated and indicated as a function of fragments atomic number in Fig. 9a and b, respectively. This figure shows that the fragment mass yield of the present formalism for  $^{238}\text{U}$  is better fitted with the experimental data [31].

Generally, high-energy photons used in photofission studies are generated through the Bremsstrahlung effect of accelerated electron beam crossing dense conversion targets. The maximum electron energy is called the end-point energy and the average compound nucleus excitation energy corresponding to such end-point energy is an important factor to reproduce the experimental data. Naik et al. [30] determined the photofission fragment mass yield for the  $^{240}\text{Pu}$  compound nucleus at 10 MeV photon end-point energy, which is equivalent to the average excitation energy equal to 7.61 MeV. In Fig. 10, the calculated results of fragment mass yield using the present formalism are compared with the experimental data. As it is clear from this figure, by considering the end-point energy instead of average excitation energy, the calculated fragment mass yield is better fitted with the experimental data.

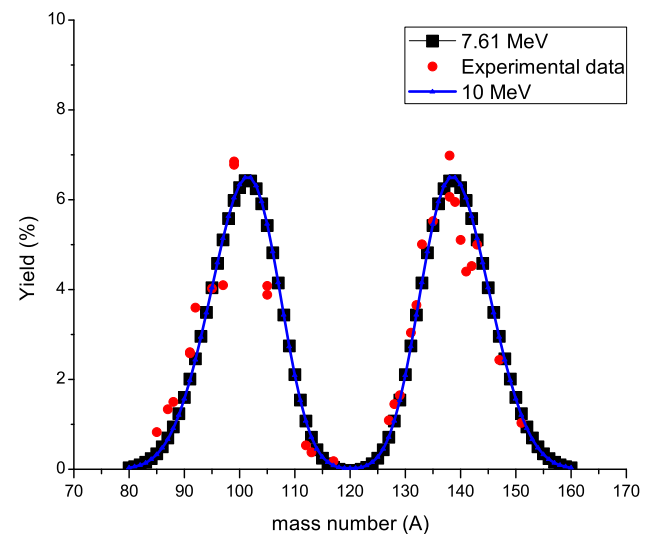
The average mass of the light ( $\langle A_L \rangle$ ) and heavy ( $\langle A_H \rangle$ ) photofission fragments for  $^{240}\text{Pu}$  and  $^{232}\text{Th}$  actinides are also obtained using the following equation

$$\langle A_L \rangle = \frac{\sum (A \times Y_L)}{\sum Y_L}, \quad \langle A_H \rangle = \frac{\sum (A \times Y_H)}{\sum Y_H}, \quad (15)$$

and the calculated results are compared, respectively, with the experimental data of Thierens et al. [27] and Naik et al.



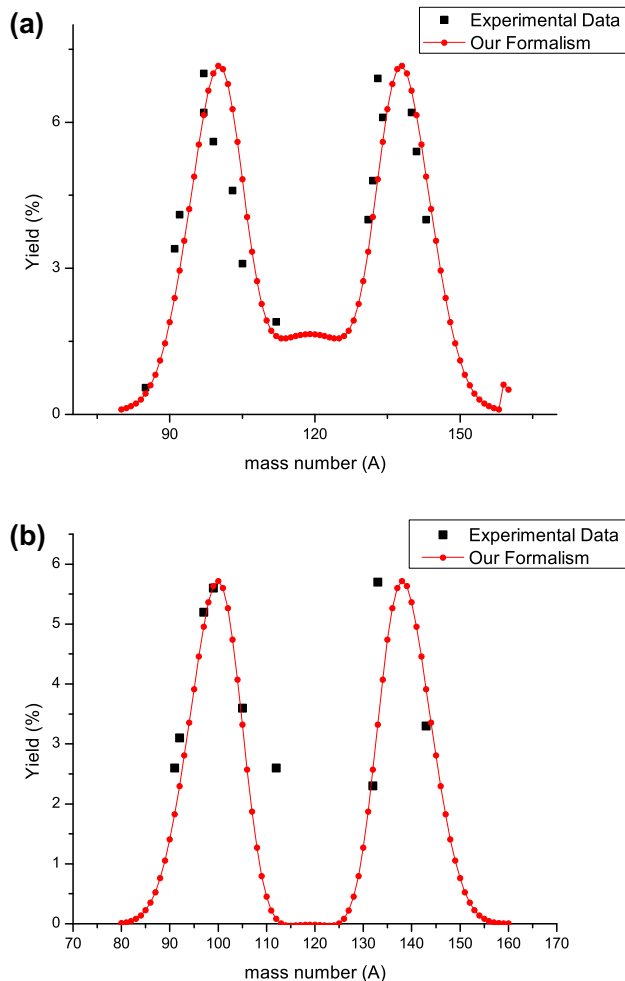
**Fig. 9** (Color online) Photofission fragment mass yield at 11.39 MeV (Figure 9a) and 13.39 MeV (Fig. 9b) for  $^{238}\text{U}$ : comparison between the experimental data [31] and the results of present study



**Fig. 10** (Color online) Photofission fragment mass yield at 10 MeV and 7.61 MeV for  $^{240}\text{Pu}$ : comparison between the experimental data [30] and the results of present study

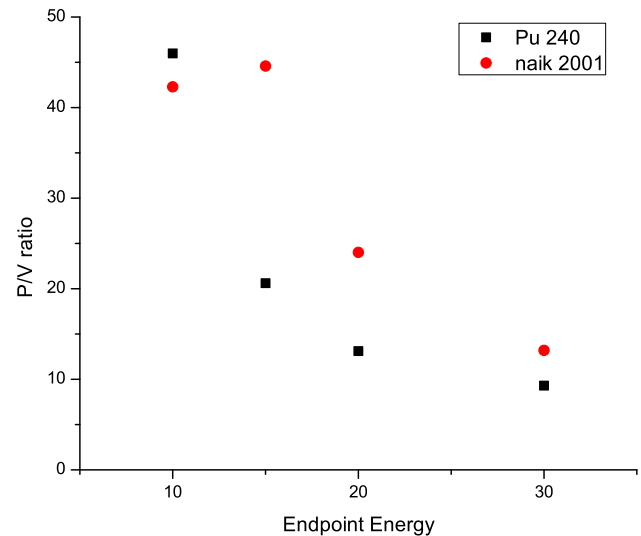
**Table 2** Average mass of the light and heavy photofission fragments for  $^{240}\text{Pu}$  at 30 MeV and  $^{232}\text{Th}$  at 80 MeV photon energies are compared with the experimental data

	Our formalism	Thierens [27]	Our formalism	Naik [28]
	$^{240}\text{Pu}$ (30 MeV)		$^{232}\text{Th}$ (80 MeV)	
$\langle A_L \rangle$	100.57	100.29	92.93	91.74
$\langle A_H \rangle$	139.42	139.71	139.14	136.75

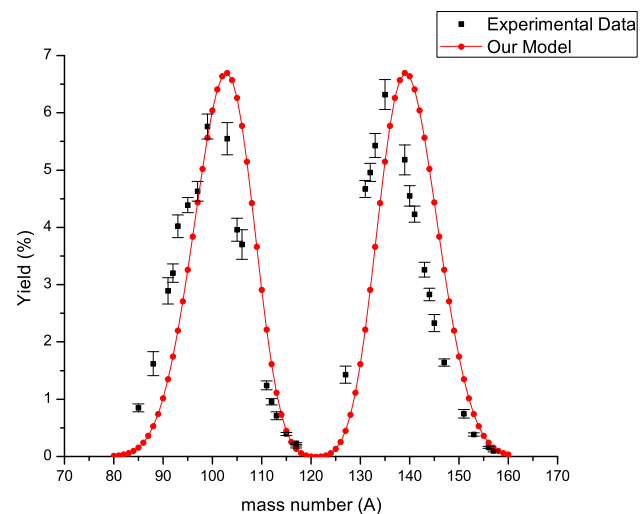


**Fig. 11** (Color online) Photofission fragment mass yield at two different high energies, 300 MeV (Fig. 11a) and 500 MeV (Fig. 11b), for  $^{238}\text{U}$ : comparison between the experimental data [29] and the results of present formalism

[31] in Table 2. As it can be seen from Table 2, there is a fair agreement between the results of our formalism and the experimental data for  $^{240}\text{Pu}$  isotope. A small inconsistency between the results of present formalism and the experimental data [28] for  $^{232}\text{Th}$  isotope is produced due to neutron emission through the fission process at high excitation energies. Photofission fragment mass yields for the  $^{238}\text{U}$



**Fig. 12** (Color online) Peak-to-valley ratio as a function of the photon end-point energies (10 → 30 MeV) for  $^{240}\text{Pu}$ : comparison between the experimental data [30] and the results of present formalism

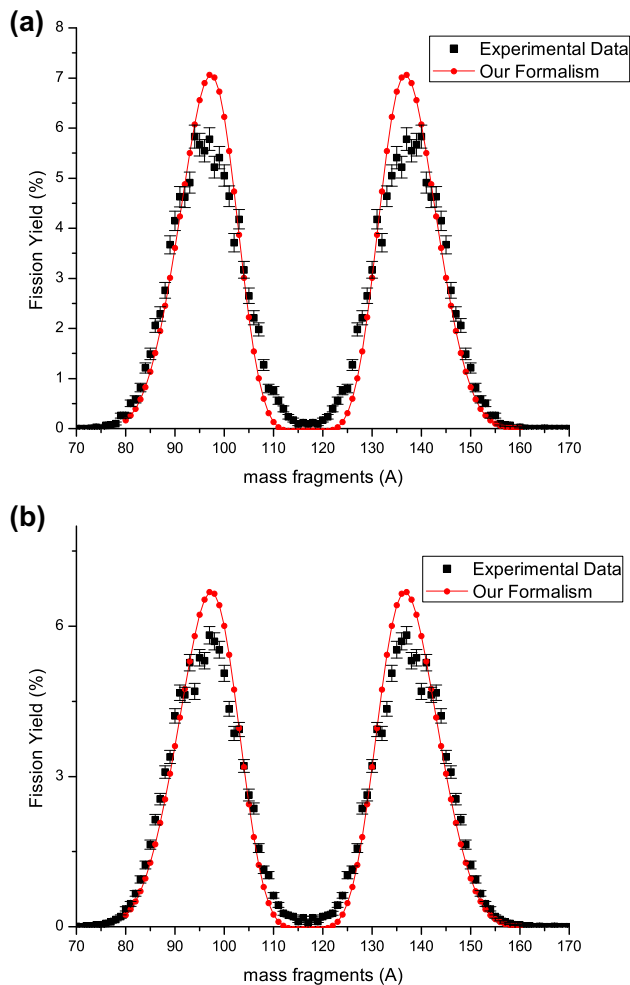


**Fig. 13** (Color online) Photofission fragment mass yield at 25 MeV for  $^{239}\text{Pu}$ : comparison between the experimental data [36] and the results of present formalism

isotope at 300 and 500 MeV are presented in Fig. 11a and b. It is clear from these figures that the calculated results of the present formalism are in good agreement with the experimental data [29]. It should be noted that the original approach of Gorodisskiy was not successful in reproducing the experimental data of high energy incident photons.

The peak-to-valley ratio of fission fragment yield for the  $^{240}\text{Pu}$  compound nucleus is calculated and compared with the experimental data of Naik [30, 32] in Fig. 12. It is clearly indicated in this figure that the peak-to-valley ratio





**Fig. 14** (Color online) Photofission fragment mass yield at 5.77 MeV (Fig. 13a) and 6.11 MeV (Fig. 13b) for  $^{234}\text{U}$ : comparison between the experimental data [39] and the results of present formalism

decreases as the Bremsstrahlung end-point photon energy grows.

The photofission fragment mass yields for the  $^{239}\text{Pu}$  isotope at 25 MeV incident photon energy and  $^{234}\text{U}$  isotope at 5.77 and 6.11 MeV energies are compared with the experimental data in Figs. 13 and 14. These figures indicate satisfactory agreement between the calculated results of present study and the experimental data except around maximum of the fragment mass yields where the results of the present formalism do not match with the experimental data properly.

## 4 Conclusion

A phenomenological formula with some adjustable parameters is developed to calculate fission fragment mass yield for  $^{232}\text{Th}$ ,  $^{234,238}\text{U}$ ,  $^{237}\text{Np}$ , and  $^{239,240,242}\text{Pu}$  actinides at various energies. Calculated results are compared with the

results of Gorodisskiy's formalism as well as the experimental data. Satisfactory agreement has been achieved between the results of the present formalism and the experimental data especially at low and intermediate photon energies. In this research, the role played by neutron emission prior to fission has also been investigated. It has been stated earlier that the present approach is not able to consider the effect of neutron multiplicity in photofission. The peak-to-valley ratio for photofission of the  $^{240}\text{Pu}$  isotope is also obtained and indicated in Fig. 12. Figure 12 shows that the values of peak-to-valley ratio is decreased with the increase in the Bremsstrahlung end-point energies. Generally, it has been shown that the calculated results of the present study are in good agreement with the experimental data as compared with the data reported in Ref. [30].

The average mass of light ( $\langle A_L \rangle$ ) and heavy ( $\langle A_H \rangle$ ) fragments for  $^{232}\text{Th}$  and  $^{240}\text{Pu}$  actinides are obtained and compared with the experimental data [27, 28]. Good agreement between the results of present approach with the experimental data has also been achieved.

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