Two-proton sequential decay from excited states of ¹⁸Ne

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Abstract Two-proton radioactivity from ¹⁸Ne is discussed in terms of sequential decay. The branch ratios for oneproton emission from excited states are calculated, which including spectroscopic factors, obtained from a Shellmodel calculation with realistic interactions. The branch ratios show that the two-proton emission from the 1⁻ state of ¹⁸Ne at 7.94 MeV is most likely to go through the sequential decay. The same mechanism is discussed for other excited states at higher energy by different interactions.

Key words Two-proton radioactivity, Nuclear shell model, Branch ratios

1 Introduction

Proton radioactivity, experimentally observed as a decay from the ground state, at GSI in 1981, has provided very important information on the structure of nuclei beyond the proton drip-line. The more complicated decaying mode, two-proton radioactivity, proposed 50 years ago in a classical article^[1] opened a investigate nucleon-nucleon new window to correlations and the structure of atomic nuclei. In 2002, the simultaneous emission of two-protons was for the first time observed in the decay of ⁴⁵Fe by Pfutzner, Giovinazzoin experiments at GSI and GANIL^[2,3]. Research in the field flourished after this breakthrough, and to date ${}^{54}Zn^{[4]}$, ${}^{48}Ni^{[5]}$, ${}^{19}Mg^{[6]}$, ${}^{16}Ne^{[7]}$, ${}^{17}Ne^{[8]}$, $^{18}\mathrm{Ne}^{[9]},\ ^{10}\mathrm{C}^{[10]},\ ^{14}\mathrm{O}^{[11]}$ and $^{29}\mathrm{S}^{[12]}$ have been found to exhibit two-proton emission. Several theoretical approaches such as Diproton model^[13,14], R-matrix approach^[15], continuum shell model^[16], adiabatic hyperspherical approach^[17], and the quantum three body cluster approach^[18], where the tunneling through the barrier is treated in a dynamical way, were applied to the problem.

There are two different decay modes for simultaneous two-proton emission: (1) three-body direct breakup involving an uncorrelated emission of the two protons, usually referred to as democratic emission. (2) ²He cluster emission where a pair of protons, correlated in a quasi-bound ${}^{1}S$ configuration, breakup, when emitted into two protons (diproton emission). The two protons have strong angular and energy correlations. The ²He appears as a resonance at 20 MeV/c in the two-proton relative momentum distribution^[19]. The microscopic calculations for the one- and two-proton decays of the 6.15 MeV 1⁻ state of ¹⁸Ne had been presented in the Ref.[20]. It was found that for the two-proton the sequential decay through a ghost of the $1/2^+$ state is within a factor of three of the observed width obtained with the assumption of democratic decay. The calculated width for diproton emission is only about a factor of two smaller than that for sequential decay indicating that the observed decay may be a combination of the two processes. In the excitation-energy spectrum of ¹⁸Ne in the Ref.[9], it's strange that some states can be seen in the two-proton emission ${}^{18}\text{Ne} \rightarrow {}^{16}\text{O+}2p$ channel and not in the one-proton emission ${}^{18}\text{Ne} \rightarrow {}^{17}\text{F+p}$ channel. That means that in these states we cannot find the ¹⁷F in ground state. So the sequential decay for two protons is most likely to occur in these states.

In this paper we present the microscopic shellmodel calculations for sequential two-proton decay from excited states in ¹⁸Ne by some different Hamiltonians.

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2 Calculation and discussion

The spectroscopic factor is the most important quantity needed to obtain the decay width. In order to calculate it, we perform a shell-model calculation to get the wave functions for ¹⁸Ne. The model space was used, including the 0s, 0p, 1s0d and 1p0f orbits. ¹⁶O is treated as a s⁴p¹² closed shell, and the low-lying positive parity states of ¹⁷F and ¹⁸Ne are taken as $s^4p^{12}(sd)^1$ and $s^4p^{12}(sd)^2$. The low-lying negative parity states of ¹⁷F and ¹⁸Ne are treated as 1 ω excitations of the form $s^4p^{11}(sd)^2$, $s^4p^{12}(pf)^1$ and $s^4p^{11}(sd)^3$, $s^4p^{12}(sd)^1(pf)^1$. So the emitted protons in the ¹⁸Ne and ¹⁷F are coming from (sd)(pf) shells. Two Hamiltonians designed for those types of model space are chosen for calculating the wave functions, namely the WBP and WBT interactions^[21]. We use a simply shell-model code by our group, in this code the spurious states are removed by the usual method^[22] by adding a center-ofmass Hamiltonian to the interaction.

The calculated excited energies of these lowlying states are shown in Fig.1. Some states are in reasonable agreement with the energies found in ¹⁸Ne. The low-lying negative states are dominated by the $s^4p^{11}(sd)^3$ configuration, but the smaller $s^4p^{12}(sd)^1(pf)^1$ component is the one responsible for one- and twoproton decay. The shell-model spectroscopic factors are obtained by the wave functions of ¹⁸Ne and¹⁷F. The decays from the positive states of ¹⁸Ne to the positive states of ¹⁷F and from the negative states of ¹⁸Ne to the negative states of ¹⁷F can go by 0d-shell wave emission or 1s-shell wave emission. The decays from the positive states of ¹⁸Ne to the negative states of ¹⁷F and from the negative states of ¹⁸Ne to the positive states of ¹⁷F can go by 0f-shell wave emission or 1p-shell wave emission. Because the $s^4p^{11}(sd)^3$ component in ¹⁸Ne is guite larger than that of $s^4p^{12}(sd)^1(pf)^1$, the spectroscopic factors are larger in the channel of positive states in ¹⁸Ne.

According to the scattering theory, the half-life for decay from initial state i to a final state f by one particle emission is given by:

$$T_{1/2} = \hbar \ln 2 / \Gamma_{i}^{if}$$
 (1)

where the decay width can be found from the relation^[25,26]:

$$\Gamma_j^{if} = S_j^{if} \Gamma_j = S_j^{if} \frac{{}^2 k \alpha_j^2}{m}$$
(2)

 S_j^{ij} is spectroscopic factor which corresponds to the probability that taking away a particle *j* with angular momentum *j* from an initial state *i*, will lead to a final state *f*. α_j is the asymptotic normalization of the proton single particle wave function in a state of spin *j*.



Fig.1 WBP and WBT predictions for the low-lying T=1 energy spectrum of ¹⁸Ne. Some levels are labeled by J^{π} and E_x . The experimental data^[23, 24] are presented on the right column. The J^{π} of levels which are not label are unknown.

The total width for decay is a sum of partial widths:

$$\Gamma^{i}_{\text{Tot}} = \sum_{jf} \Gamma^{if}_{j} \tag{3}$$

The branching ratios are simply the ratio between a partial decay width and the total one:

$$Br^{if} = \frac{\sum_{j} \Gamma_{j}^{i}}{\Gamma_{Tot}^{i}}$$
(4)

For the fourth 1⁻ state at 7.94 MeV in ¹⁸Ne, we find that the spectroscopic factors decaying to the $1/2^-$ third excited state ($Q_{1p} = 0.914$ 1 MeV) is quite larger than that decaying to the $5/2^+$ ground state ($Q_{1p} = 4.018$ 4 MeV) of ¹⁷F. The spectroscopic factors and the widths for each of the channels are shown in Table 1. In this table, we can find the branch ratio that decays to $1/2^-$ state is larger than those decays to the ground state and the first ground state because it has

larger spectroscopic factor even though it has smaller single-particle width. We can conclude that the 7.94 MeV 1⁻ state is most likely to be the best candidate for two-proton sequential decay. That is why it can be seen in the two-proton emission channel and not in the one-proton one. There are other states in this situation, like the 3⁻ state around 9–10 MeV (9.809 MeV for WBP and 10.099 MeV for WBT) and the 5⁻ state near 13 MeV (13.412 MeV for WBP and 13.200 MeV for WBT).

Table 1 Spectroscopic factors from the state $J^{\pi}=1^{-}$ of ¹⁸Ne at $E_x = 7.94$ MeV. The channel $5/2^+ \otimes 0f7/2$ means that the emitted proton is from the 0f7/2 shell and decay to the $5/2^+$ state in ¹⁷F. The last line is the total widths for single-proton

	WBP	WBT	Expt.	
$E_{\rm x}$ / MeV	7.648 0	7.698 6	7.94	
Channel	Spectroscopic factor			
	WBP	WBT	Γ_{sp} / keV	
$5/2^{+} \otimes 0$ f7/2	0.010 61	0.003 52	129	
$5/2^+ \otimes 0 f 5/2$	0.010 11	0.007 65	101	
$5/2^+ \otimes 1p3/2$	0.001 01	0.004 28	2 818	
$1/2^+ \otimes 1p3/2$	0.003 34	0.002 23	2 239	
$1/2^+ \otimes 1p1/2$	0.000 13	0.000 13	2 188	
$1/2^- \otimes 0d3/2$	0.001 06	0.005 25	2	
$1/2^- \otimes 1s1/2$	0.091 86	0.240 19	122	
	Γ_{WBP}	Γ_{WBT}	Br _{WBP}	Br _{WBT}
$5/2^+ \otimes (0f+1p)$	5	13	0.216	0.277
$1/2^+ \otimes 1p$	8	5	0.32	0.11
$1/2^- \otimes (0d+1s)$	11	29	0.464	0.613
Total Γ	24	47	Expt. \leq 50 keV	

3 Conclusion

We have presented some preliminary results of the proton decay branch ratios and decay width in ¹⁸Ne using a shell-model calculation. The results obtained for the branch ratio from the 1⁻ state at 7.94 MeV in ¹⁸Ne show that this state is most likely to be a candidate for sequential two-proton decay. The 3⁻ and the 5⁻ states can also be candidates for the same process.

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